

Article

A Contextualised General Systems Theory

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1 **Abstract:** A system is something that can be separated from its surrounds, but this definition
2 leaves much scope for refinement. Starting with the notion of measurement, we explore
3 increasingly contextual system behaviour, and identify three major forms of contextuality
4 that might be exhibited by a system: (a) between components; (b) between system and
5 experimental method; and (c) between a system and its environment. Quantum Theory is
6 shown to provide a highly useful formalism from which all three forms of contextuality
7 can be analysed, offering numerous tests for contextual behaviour, as well as modelling
8 possibilities for systems that do indeed display it. I conclude with the introduction of a
9 Contextualised General Systems Theory based upon an extension of this formalism.

10 **Keywords:** context; complexity; quantum-like models; non-separability

11 1. Systems Theory in a Crisis?

12 Systems Theory has reached something of an impasse. While early work yielded a range of insights
13 about general system behaviour [1,2], the field has failed to live up to this early promise. Indeed, the
14 periodic rise and fall of interest in cybernetics, systems, complex systems, and now complex adaptive
15 systems suggests that the field is hitting a barrier that it is struggling to overcome. Here, I will argue that
16 re-examining the notion of context can help us to progress.

17 We will start with a consideration of the very notion of a system. What allows us to model some
18 part of the world as a system, separate from its surroundings? This will lead to a discussion of the
19 idea of a measurement that can be performed upon a system. At this point we shall see that only a
20 very small subset of systems displays objective behaviour upon measurement. This observation allowed
21 entire fields to progress in their attempts to understand reality, however, the systems modelled by fields
22 such as physics and chemistry are not all there is to reality; we must be very careful as to how deeply

23 we hold the idea that objective responses to measurement are essential to the very idea of science. Many
24 systems do not display such behaviour, and it is essential that we understand the different ways in which
25 they can violate what might otherwise be regarded as a core tenet of science.

26 The attempt to understand this violation of objectivity will form the core contribution of this work. We
27 will consider the notion of context, and the way in which contextual behaviour leads to the manifestation
28 of behaviour that is often denoted as complex. Contextual behaviour has been witnessed in physics too,
29 and Quantum Theory (QT) was the result. QT has developed a whole range of formalisms to describe
30 contextuality, but there is no *a priori* reason why these cannot be used beyond the domain of physics.
31 Indeed, a new field of research has sprung up from the attempt to create *quantum-like* formalisms to
32 describe the behaviour of systems exhibiting contextual behaviour.

33 However, stepping back from this general modelling paradigm it is possible to realise that QT did not
34 cease with the standard formulation of quantum mechanics. The description of structures appearing and
35 disappearing required a move to Quantum Field Theory (QFT), historically through the mechanism of
36 second quantization, but this is not the only path available, as demonstrated by the Functional Methods of
37 QFT [3]. A more direct set of mappings should be sought in any attempt to describe complex emergent
38 systems, and we shall discuss the manner in which this might be achieved in within the framework of a
39 Contextualised General Systems Theory (CGST).

40 We begin with the notion of a system.

41 1.1. What is a System?

42 At its simplest, a *system* \mathcal{S} is a set of entities that are interacting via a set of relationships [4]. It is
43 something that we can single out from some sort of *environment* \mathcal{E} , and is designated as either *closed* or
44 *open* depending on whether it interacts with that environment. Some fields of science have discovered
45 a dynamics (or set of laws) that describe their systems, but other fields have been finding it harder to
46 discover even the requisite underlying kinematics (or general behaviour) of their systems of interest.
47 Here, we shall take the notion of *separability* to be key to the definition of a system. Such a move is
48 hardly unique, indeed, both the Latin word *systema*, and the Greek word *σύστημα* have this same notion
49 of a set of components which form something distinct from their surrounds. This concept went on to
50 motivate the very notion of *reduction*, which is central to the basic understanding of science [5,6], and
51 yet, many different fields have challenged this fundamental notion of separability. Thus, we see scenarios
52 such as biological systems which display phenotypic plasticity, and so depend not just upon their genetic
53 sequences, but upon the environment in which they evolve [7,8], and people who give responses to
54 questions about the length of a line which depend upon the responses that have been given before by a
55 set of conspirators [9]. Even that bastion of reduction, physics, has shown what might be regarded as a
56 surprising tendency to throw up contradictions when we assume that reductive models of the Universe
57 will prove appropriate, with phenomena like entanglement/non-locality [10], colour confinement [11,12],
58 and collective dynamics [13], all presenting their challenges to reductive explanations.

59 Some examples will serve as guiding illustrations for the arguments that we will develop here.

60 **A tennis ball** is notably distinct from its environment. If we know the mass of the ball, its initial
61 velocity, and the value of gravity then we can easily map out the trajectory of a system such

62 as this (and a school student is frequently expected to do so). Indeed, the movements of objects
63 like this very much motivated the development of modern physics (and so our conceptualisation
64 of science). However, even an example as simple as this one becomes problematic upon closer
65 examination. Gravity changes in different places, friction becomes important (in the form of air
66 resistance), and even the surface of the ball can affect its trajectory. Of course these effects are
67 second order, and we only care about them in the case where a highly accurate prediction about
68 where the ball falls becomes necessary. However, a projectile that is moving fast enough requires
69 an entirely new theory, General Relativity, in order to reach the accuracy required in some cases
70 (e.g. when we are trying to estimate where satellites will be for our global GPS infrastructure).
71 Thus, even in the paradigmatically simple case of projectile motion, there is no one model or
72 theory that universally applies.

73 **A steam engine** provides a slightly more complex example due to its internal mechanisms which are
74 dependent upon thermodynamic principles. Measurements can still be performed upon such a
75 system, and depending upon how well it is isolated from the environment we will see well defined
76 behaviour emerge. Much of modern statistical mechanics arose from relaxing conditions about
77 how isolated a system is from its environment (with the formalism describing microcanonical,
78 canonical and grand canonical ensembles as the system becomes more open). One particularly
79 new aspect presents upon comparison with our original tennis ball; steam engines can exchange
80 material with their environments, and so should no longer be regarded as closed. Indeed, as long
81 as a steady supply of combustible material is maintained the steam engine will enter a steady state,
82 where the energy it produces becomes a constant (despite requiring this constant input).

83 **Biological systems** are more difficult to separate from their surrounding environment. An organism,
84 while distinct, and following physical laws (such as the same gravitational laws affecting the
85 tennis ball) *must* interact with its environment in order to survive. It is an open system, and is
86 generally considered to be dissipative [14] (in contrast even to systems described by the grand
87 canonical ensemble which is assumed to be in equilibrium). This means that biological systems
88 rely in principle upon the environment to ensure their ongoing structural and functional stability,
89 and their models tend to make this openness more explicit than is the case for statistical mechanics.
90 Biological systems are also inherently contextual, with genes, species, and even ecosystems
91 capable of exhibiting profoundly different responses to the same stimulus if it occurs within a
92 different context [15]. These characteristics already make the notion of a system very different in
93 biology compared to those that are commonly considered in physics.

94 **Language** arises within a population in a society, and so it makes almost no sense to talk about the notion
95 of a system and its environment in this case. However, structurally, language is frequently assumed
96 to be separable, at least at the syntactic level. Indeed, a centrally held dogma in linguistics,
97 the principle of compositionality, states that the meanings of higher order expressions such as
98 sentences are determined from a combination of the meanings of its constituent parts [16]. If this
99 principle were true, then it would imply that linguistic systems can be straightforwardly separated
100 from their surrounding environment, however, it is very difficult to justify either theoretically
101 or empirically. The social nature of language implies that the meaning we attribute to words is

102 probabilistically modified not just by other words [17], but also by our experiences, education,
103 social identity, demographics and our current context. As a result, fields such as cognitive science
104 still struggle to produce models of language that incorporate well known effects.

105 **Societies** exhibit a wide range of complex interdependencies. For example, social psychology has
106 developed a highly sophisticated understanding of the complexities inherent in human interactions,
107 with phenomena like cognitive dissonance, attitude change, prejudice, the conceptualisations of
108 self and identity, and the formation of ideologies all subject to intensive investigation [18]. Most
109 of these studies consistently reveal strong interdependencies between the system under study and
110 the environment. Should we draw our separating line around the people in the society? Should we
111 include their technology and domesticated animals? What of the way in which different societies
112 change their terrain (e.g. by draining swamps, deforestation, the emission of carbon, etc.). It
113 is difficult to find a clear dividing line between a society and its environment. Social factors
114 also affect the individual. For example, Asch's line judgement task [9] shows that the context in
115 which people make judgements even about the length of a line can be profoundly affected by their
116 social context. This makes it highly difficult to draw a clean line around a social system; even
117 the experimentalist can have a strong influence upon a social system, with issues such as framing
118 [19] showing that how you ask a question can profoundly affect the result that you obtain from a
119 subject.

120 Of course, many different behaviours can be described by the tools developed in physics, which
121 suggests that the framework of system plus environment ($\mathcal{S} \oplus \mathcal{E}^1$) is remarkably useful. For example,
122 Albert and Barabási [20] have combined Network Theory and Statistical Mechanics to describe some
123 characteristics of biological, linguistic and social systems. However, the characteristics of the systems
124 described by models such as these are not particularly complex [21]; are we selecting for those
125 behaviours that we *can* model using these techniques?

126 1.2. General Systems

127 General Systems Theory (GST) attempts to specify a set of principles that can apply to all types
128 of systems [1]. Its history traces back to attempts to respond to the challenges posed by non-physical
129 (e.g. biological, cognitive and social) systems to our reductive techniques [2]. Indeed, von Bertalanffy's
130 attempt to argue for a 'middle way' perspectivism between absolutism and radical relativism [2] suggests
131 that GST arose from an acceptance that the full set of behaviour and properties pertaining to some
132 objects might be difficult to describe using models that derive purely from physics. Von Bertalanffy
133 argued that biology needed not just empirical "facts", but hypotheses and eventually laws of some form.
134 However, this raises an important problem, biological systems are inherently *contextual* (as are many
135 cognitive and social systems), which makes many of the tools of the modern scientific method very
136 difficult to apply. The assumption that these systems can be described as objects, behaving objectively

¹ This is a general notation, referring to a general system with two components. The \oplus symbol is meant to be general, and does not refer to a direct sum in any way.

137 (i.e. independently of the manner in which we observe them) becomes highly problematic [15,21],
138 and so assumptions routinely used in physics begin to lose their validity. Separability, reduction and
139 independence between components increasingly find themselves questioned, and new notions become
140 important, including emergence, holism, and downward causation [6,22–24].

141 However, formalising these notions has proven to be difficult. Instead of a generalised formal model,
142 we have seen a range of different approaches and methods proposed, especially as GST was gradually
143 replaced by Complex Systems Science (CSS). Network Theory; Agent Based Modelling; Statistical
144 Models; Spin Glass models; and Evolutionary Approaches have all been applied to the modelling of
145 systems well beyond the physical [25,26]. However, caution is necessary. Von Bertalanffy noted the
146 difference between “description” and “explanation”, bemoaning the fact that biology was stuck in a
147 descriptive, or pre-Copernican period [2], which could provide an explanation for this wide range of
148 models and approaches. Are we stuck in a descriptive phase? Or do we *require* multiple models?

149 1.3. Model Complexity

150 The complexity required of a model depends not just upon the system to be described. The
151 requirements of the modeller also play a role.

152 Even for the case of the tennis ball we saw that varying levels of model complexity were possible.
153 However, in that case it was possible to choose between them according to the *accuracy* of model
154 required. This is because tennis balls exhibit a clear boundary separating the ball from its environment,
155 which means that it is only necessary to consider those factors in the environment are required for an
156 accurate enough description of its dynamics. This relatively straightforward scenario can be contrasted
157 with other systems which do not display such a clear separation. In particular, it is frequently the case
158 that different *levels of description* are possible within the one system. Thus, in the case of an ecosystem
159 we see that:

160 *Depending on the spatiotemporal scale or window through which one is viewing the world,*
161 *a forest stand may appear (1) as a dynamic entity in its own right, (2) as a constant (i.e.,*
162 *nondynamic) background within which an organism operates, or (3) as inconsequential*
163 *noise in major geomorphological processes. O’Neill et al. [27, p83]*

164 Of course this emphasis upon levels of description is by no means new. For example, in cognitive
165 science, Marr proposed that three complementary levels of analysis should be used to understand
166 information processing systems: (i) computational; (ii) representational and algorithmic; and (iii)
167 implementational [28]. These levels can respectively be understood as the function, procedures
168 and physical mechanisms of the cognitive system [29]. In both Marr’s approach to understanding
169 information, and the scenario described by O’Neill *et al.* [27] we see that the scale used to model the
170 forest stand depends upon the requirements of the modeller. Is a botanical, zoological, or geological
171 model required for the forest stand? Alternatively, are we seeking a algorithmic, functional, or hardware
172 driven model of cognition? Different modellers are interested in different aspects, or *perspectives* of
173 the same system [29]. Indeed, this form of argument can be traced back to at least Aristotle’s four
174 classifications of cause: material; formal; efficient; and final [24], each describing different causal
175 categories that can be used in the explanation of some general thing (be it object, relation, law etc.).

176 Such levels of description pose a challenge to the more standard definitions of complexity, which often
177 list a series of properties that are displayed by complex systems. For example, Mitchell [25] suggests
178 that complex systems must exhibit: (i) Complex collective behaviour; (ii) signalling and information
179 processing; and (iii) adaptation. While this is by no means a poor definition, it fails to acknowledge
180 the contextuality of the very definition of a system as complex. Returning to the forest stand example
181 above, these characteristics are only exhibited when it is the forest itself that is under study. In a larger
182 scale model (say of an ecosystem, which is usually also regarded as complex by this kind of a definition)
183 the complexity of the forest stand often disappears, to be replaced by a very simple model. Thus, for
184 the system under examination by O'Neill *et al.* [27] the forest stand is modelled as a simple random
185 noise term in comparison to major geomorphological processes, and by a constant factor when it is
186 the species living inside the forest under consideration. Neither of these models would be considered
187 complex according to the definition of Mitchell [25]. If the forest were something that we had never
188 been interested in then we would never have thought to designate it as complex. So, while more is no
189 doubt different [30], it seems inappropriate to designate a system as either simple or complex without
190 consideration of the level at which it is to be understood. Indeed:

191 *the way we look determines what we see, or rather it co-determines the latter, in conjunction*
192 *with what there is.* Kampis [31, p95]

193 But this raises an interesting question; how are we to analyse such contextual complexity?

194 For many systems the decision as to which level of description should be adopted depends upon the
195 observer, who is required to make an *epistemic cut* between the system and the environment [32]. There
196 are very few systems with a natural cut, and historically most of them were found in physics, which
197 appears to have a very special status in modelling. Thus, many of our approaches to modelling (and our
198 associated assumptions) have been derived from a field in which such separations are generally assumed
199 to be possible (and historically have been). However, even in physics, assumptions of noncontextuality
200 and separability have become problematic. It is often the case that in examining complex systems we are
201 far more than passive observers. Yet we have very few theoretical tools that can represent such behaviour.

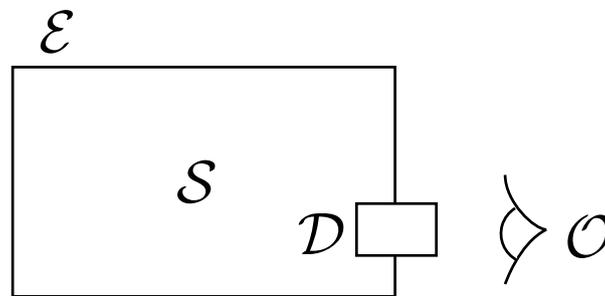
202 However, our understanding of the role of the observer suggests that understanding measurement is
203 key to understanding contextuality. For this reason, we shall now turn to a consideration of measurement.
204 In what follows we shall gradually increase the contextuality of the behaviour revealed by measurement,
205 asking what this tells us about the formalism required to understand and model the resulting behaviour.

206 **2. Measuring General Systems**

207 In order to describe measurement, we will have to enlarge our notion of a system. Measurements
208 form a boundary between the system and the environment (in which the observer traditionally resides).
209 Introducing both the observer \mathcal{O} and a measuring device \mathcal{D} leaves us with the more specific system
210 shown in Figure 1, one that it is possible to experimentally probe and investigate.

211 The classical ball, moving according to the laws of Newtonian physics must hit a device of some
212 form to be measured. This could be a wall, a basketball hoop, a net, tennis racket etc. but will
213 inevitably require an interaction between the system and the device. While the ball has a well defined
214 position before measurement (which could be extracted using visual observation) this does not count as

Figure 1. At its simplest, a system \mathcal{S} is something that can be considered as distinct from its environment \mathcal{E} in some manner. Some systems can be measured by a device \mathcal{D} which discovers information about the state of the system, and reports it to an observer \mathcal{O} who resides in the environment.



215 a measurement due to the way in which perceptual stimuli can be easily misjudged in scenarios of bias.
 216 Nonetheless, it is possible to straightforwardly assume that the ball *has* a position before it is measured,
 217 and that the measurement merely finds out what it was (in an objective manner, as photons reflected from
 218 the ball are incident on the eye). Measurement merely records reality, it does not influence what is found
 219 during that measurement.

220 Such assumptions, while sometimes correct, can be markedly dangerous. For example, assuming that
 221 a photon can be described in the same way as the tennis ball results in surprise. Consider for example
 222 the modern quantum version of the Young's double slit experiment, which reveals interference patterns
 223 even when single electrons are sent into the apparatus [33], unless a measurement is performed at one of
 224 the slits to find out which way it went (in which case a diffusion pattern results).

225 Further afield, the concept of a 'gene' in biology has moved from protein coding sequences to a
 226 more modern understanding that genes are comprised of many interdependent elements, and that this
 227 makes it very difficult to delimit even the boundaries of a gene. Even when classically conceived, it is
 228 not clear where the boundary between selective units and their environments lie. A gene is subject to
 229 its environment, but this includes not only its cellular and extracellular environment, other genes and
 230 regulatory elements, homologues etc. are also important. Increasingly we see the notion of functional
 231 genetic units expanding to include network modules, rather than just genes [34].

232 Similarly, in psychology and sociology, we find that the way we ask questions inevitably affects the
 233 response that we obtain. For example, framing a question in a positive or negative light can result in
 234 statistically significant preference changes, even if the same question is being asked [19].

235 Systems such as these pose problems for any theory which assumes that a system 'has' objectively
 236 defined properties, without reference to the context in which these occur (which could be a measurement
 237 scenario, an environment, another confounding measurement etc.). Thus, an organism does not have a
 238 phenotype without reference to its environment, and a wide range of experimental data shows that it is
 239 highly problematic to assume that attitudes, opinions, affect and decisions can be measured objectively
 240 (i.e. without reference to the social context in which they occur). This *contextuality* presents many
 241 problems for the modeller. A context cannot be something that is within the system (\mathcal{S}), rather, it
 242 is beyond the thing that was originally designated as interesting. Conversely, a context is somehow
 243 interesting in its own right, it is not something that should be relegated to an environment (and by

244 implication deemed uninteresting). However, this leaves us in an awkward position, what is a context
245 precisely? This question is not one that has been satisfactorily answered from a systems perspective. The
246 factors that have been termed a ‘context’ are more diverse than the fields that utilise the term. Sometimes
247 a context is a location (e.g. in mobile technologies), sometimes it is a set of parameters (e.g. when a
248 context is stored during a task interruption), a context might indicate how much information is assumed
249 by the members of a culture (in anthropology), or the words that influence the semantic association a
250 subject gives to another word (in linguistics). This list is by no means exhaustive. Context appears to
251 be a grab bag term, used to denote something that is interesting, but not really a part of the originally
252 envisaged system.

253 This variety of different uses often results in category errors. Much of what we call contextual can
254 be reduced to an extra parameter in model (e.g. the location of a mobile device). Such data exists out
255 there, we do not know it, but it has a well defined value. This calls into question the original designation
256 of such a factor as contextual. If this data is relevant to the description of the system of interest then
257 we have drawn our boundary incorrectly (in this case around the mobile phone, opting for a model that
258 is primarily influenced by the boundaries of objects, instead of the more abstract model that described
259 the object in a location). Note that the biotic system that is placed in a different environment is not of
260 the same form. It is impossible to be sure what form the phenotype will have as it depends upon an
261 interaction between the system and the environment, and here we find an important clue. Contextuality
262 must be ontological. That is, it must refer to fundamental uncertainty that is displayed by the system
263 once a level of analysis has been designated.

264 Very few tools have been developed for the description of contextual behaviour. This problem is
265 compounded when we consider the manner in which this behaviour manifests; it is often the case that
266 our very attempts to measure, model or interact with a contextually dependent system result in a change
267 to the very results obtained from our measurements of that system (not just its future dynamics). Consider
268 the way in which the assumption that the global financial market was crash free led to the Black–Scholes
269 model, which itself precipitated the 1987 stock market crash [35]. Here we see a situation where the
270 model adopted to describe a system affected its very dynamics, i.e., in *incorrectly assuming* that the
271 economy was separate from the scientific process of its analysis and description, the very model created
272 to describe the dynamics of the stock market became responsible for a change in its dynamics.

273 There appear to be a number of different classes of contextuality which might be displayed by a system
274 of interest. We might initially expect that different effects would result from contextual responses:

275 **(a) Between components** where the responses of one component will depend upon input from other
276 components of the system. Consider for example the genetic pathways that can be identified in
277 different cellular responses to stimuli [36]. These depend very heavily upon the prior activation of
278 the different genes involved; the same response will not always be exhibited in response to what
279 appeared to be the same input. In a different context very different results might occur. As this
280 is a dependency that arises within the traditional boundaries of a system there are already many
281 techniques that can be utilised to analyse this form of contextuality. Indeed, many complex system
282 approaches, such as network models [34,37] and agent based modelling (ABM) [38,39] already
283 provide a useful framework for the investigation of such inter-component dependencies, although
284 more work will obviously be necessary to develop a full understanding of them [40].

285 **(b) Between system and experimental method** where our theories are consistently failing [21,41]. As
286 an extreme example we can consider the problems of framework and subjectivity that often beset
287 social scientists; how they look at social systems often determines the results that they obtain
288 [42]. However, we might also consider the complexities inherent in scientifically describing
289 economic responses [35], social interactions [43], psychological diagnoses and outcomes [44],
290 as well as our understanding of language, semantics and meaning [45]. Many complex systems
291 display highly contextual responses to the method used to analyse them, and this has hindered their
292 description by scientific approaches. Indeed, there are very few formalisms capable of describing
293 such experimental contextuality.

294 **(c) Between system and environment** context can result in profound effects. One classic example
295 is provided by the phenomenon of phenotypic plasticity where two organisms with identical
296 genotypes can yield phenotypes so different in two different environments that they are identified
297 as different species [46]. Indeed, Theoretical Biology could be identified as one of the key
298 areas in which GST developed a wide range of models that sought to understand environmental
299 contextuality (e.g. [1,24,47,48]).

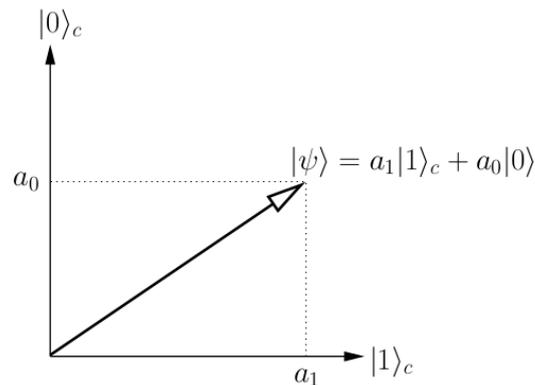
300 These different contextual responses may require different modelling methodologies, but it might also
301 be possible to generalise our understanding of context from a proper consideration of their similarities.
302 While contextual dependencies between components are the focus of much current Complex Systems
303 Science (CSS) research, less work looks at contextual dependencies of type **(b)** and **(c)**. Given the
304 apparent prevalence of contextually dependent complex systems in our modern world, one might wonder
305 at the apparent lack of theories capable of modelling such behaviour. One way forward would involve
306 taking contextuality seriously. Intriguingly, one formalism already exists which takes contextuality
307 between a system and experimental method very seriously; Quantum Theory.

308 **3. Contextuality in Quantum Systems**

309 Context matters in the formalism of Quantum Theory (QT). From von Neumann's measurement
310 theory and the Heisenberg Uncertainty relations [49], to the Bell and Kochen–Specker theorems [49,50],
311 the context of a quantum system plays a vital role in the results we obtain when we try to measure its
312 properties and behaviour.

313 This implicit recognition of context in standard quantum measurement theory can be quickly
314 demonstrated. According to the formalism (see below for more details) the probability of some
315 measurement outcome can be extracted by representing the state of the system ($|\psi\rangle$) with respect to
316 some *measurement context*. Thus, in figure 2, we see a simple measurement of a system which answers
317 a basic yes-no question (e.g. did the particle go up or down when we measured its spin). We represent
318 this scenario using a measurement context c which consists of a subspace in which the state $|\psi\rangle$ can
319 be embedded. We use an orthonormal basis $\{|1\rangle_c, |0\rangle_c\}$ to model this subspace, where the two vectors
320 $|1\rangle_c$ and $|0\rangle_c$ are used to represent the measurement of yes or no in the context c . QT predicts that the
321 probability of recording a yes to our question in context c is equal to the square of the projection of $|\psi\rangle_c$
322 onto the $|1\rangle_c$ state, and the probability of recording a no is equal to the square of the projection of $|\psi\rangle$
323 onto the $|0\rangle_c$ state. This is a geometrical account of probability, given by a straightforward application

Figure 2. A state $|\psi\rangle$ is represented by the quantum formalism within a context. For this simple illustrative example, we see the state represented within a context c , which is drawn in a two dimensional space, spanned by the basis $\{|1\rangle_c, |0\rangle_c\}$. This context could represent the probability of a yes ($P(yes_c) = |a_1|^2$) or a no ($P(no_c) = |a_0|^2$) result being recorded upon the measurement represented by c . Changing the context of the system can be represented by rotating the basis, and would lead to different projections of the state onto that new context.



324 of Pythagoras theorem [49]. The result is a remarkably different understanding of probability when
 325 compared to the more standard epistemological approaches which take probability as arising due to a
 326 *lack of information* (i.e. knowing too little about what a state of affairs actually is). A geometrical
 327 account of probability allows for a particularly natural representation of how a system might respond
 328 to a change in context (when a state of affairs becomes ontologically different). Thus, a rotation of the
 329 $\{|1\rangle_c, |0\rangle_c\}$ basis could represent a different context (e.g. rotating the spin measurement apparatus), and
 330 different probabilities would result.

331 This intuition can be formalised, as follows. First, $|\psi\rangle$ is written in terms of a set of basis states, $\{|\phi_i\rangle\}$.
 332 This representation of $|\psi\rangle$ is obtained by expanding it as a linear superposition (i.e. an appropriately
 333 weighted sum) of one set of basis states (commonly obtained in practice through reference to the *choice*
 334 of apparatus and its orientation, state *etc.* and written as an orthonormal basis, although this is by no
 335 means essential). We find that $|\psi\rangle = \sum_i c_i |\phi_i\rangle$ where the weight terms c_i represent the contribution
 336 of each component ($|\phi_i\rangle$) of the basis to the actual state. The choice of basis states is governed by the
 337 observable to be measured and the quantization procedure that relates each observable, A , to its quantum
 338 counterpart, \mathbf{A} [49,51]. Perhaps most importantly, the standard interpretation of quantum theory claims
 339 that upon measurement the quantum system is found to ‘collapse’ onto one of the eigenstates associated
 340 with the eigenvalue equation $\mathbf{A}|\psi\rangle = \lambda_i|\psi\rangle$. Hence, upon measurement a non-linear outcome occurs
 341 due to this process of collapse, which is related to both the state of the system, and to the context of that
 342 system (as it is represented by the observable). Further experiments will then be performed upon this
 343 newly collapsed state, and so later measurements will also be affected. We see that the probabilities of
 344 QT arise not from a lack of details (as is the case for standard Kolmogorovian probabilities), but rather
 345 from the geometrical representation of a state that is implied by QT’s formal recognition of context in the
 346 process of measurement [49].

347 This simple approach to the modelling of measurement means that the quantum formalism
 348 incorporates the experimental context of a system into its description of that system, and this context
 349 can profoundly affect the experimental result obtained. Thus, QT can describe system contextuality of
 350 type **(b)**. This is a highly unusual state of affairs in scientific modelling, which almost by definition
 351 assumes that a system of interest can be separated from the models that are used to analyse its behaviour.

352 The generalisation of QT beyond the physical realm would make it possible to model similar
 353 contextual effects in systems not presently well modelled by the scientific method. Indeed, this
 354 process has begun already, quantum inspired models have already been used to model a wide range of
 355 non-physical systems [52,53], including: decision making [54–58]; attitude change [59]; language and
 356 memory [60–63]; biology [15,64–66]; creativity and cultural evolution [67,68]; vision [69]; economics
 357 [70,71]; and information retrieval [72–74], to name just a few examples.

358 3.1. Non-separability and Openness in Quantum Models

359 In addition to this immediate application to the description of contextual measurements, the
 360 phenomenon of *entanglement* [49,51,75] allows us to extend the quantum formalism to the description
 361 of systems exhibiting contextual dependency of type **(a)**. If we consider two components S_A and S_B
 362 of a system S , then a contextual dependency between the two implies that it is not possible to consider
 363 them separately. The quantum formalism provides a very clear description of this state of affairs. If
 364 we denote the states of the two components by $|\psi_A\rangle$ and $|\psi_B\rangle$, then a separable combined system,
 365 $|\psi_{A\oplus B}\rangle$, will be one that can be decomposed using a tensor product²: $|\psi_{A\oplus B}\rangle = |\psi_A\rangle \otimes |\psi_B\rangle$. In
 366 contrast, a system for which the components cannot be considered independently is represented in
 367 the quantum formalism using an entangled state. Thus, if for example component S_A always exhibits
 368 response a when S_B does, and response b when S_B does then we might represent the combined system
 369 as $|\psi_{A\oplus B}\rangle = \mathcal{N}_1|aa\rangle + \mathcal{N}_2|bb\rangle$ where \mathcal{N}_1 and \mathcal{N}_2 take the role of some normalisation factor (i.e.
 370 $\mathcal{N}_1^2 + \mathcal{N}_2^2 = 1$). If such a state is impossible to represent as a tensor product, then it is deemed
 371 non-separable, and termed *entangled*. Entangled states are responsible for many of the counter-intuitive
 372 results of QT [75], but most interestingly to the current argument, they exhibit contextual responses to
 373 measurement [76,77] where they play an essential role. According to the standard interpretation of QT,
 374 a measuring device must first become entangled with the system of interest before collapse occurs and a
 375 result is obtained [49]. This suggests that systems of type **(a)** and **(b)** in fact share the same dynamics.

376 Finally, contextual dependencies of type **(c)** can sometimes be modelled using dissipative, or open,
 377 quantum models [78,79]. These systems are subject to ongoing interaction with their surroundings
 378 (which at a first approximation can be treated as a measurement), and so the complexity of their dynamics
 379 increases substantially. While some work has been completed which uses this formalism in quantum-like
 380 models (e.g. [58,66]) this is a new and fast developing field. Open quantum systems are made even more
 381 interesting by the way in which they are often related to ontological models of emergence. For example,

² In what follows we will use a standard formalism where \oplus is used to denote the combination of two systems via a general operator (i.e. it is not necessarily an addition operation) whereas \otimes denotes the specifics of a tensor product which can be used to model this combination when the system is technically separable.

382 Vitiello has modelled the contextuality of memory using an open quantum model [13]. As many complex
 383 systems are generally open to environmental influences this is an area that is likely to become the focus
 384 of much future work.

385 Thus, we see that the three forms of contextuality introduced in section 2 can be accommodated
 386 within a consistent set of models inspired by the quantum formalism. What more specific tools does QT
 387 provide? Could these be used in a Contextualised General Systems Theory?

388 3.2. Tests for Contextuality

389 There are a wide range of contextuality effects in QT. In this section we will start with a class of tests
 390 that can be used on systems with one component, and then gradually increase the system complexity, by
 391 adding more components, and the possibility of interactions between those components. We shall see
 392 that QT has provided an entire class of tests which can be used to determine the validity of the assumption
 393 that a system is non-contextual. Violations of the Law of Total Probability, Bell's theorem, the
 394 Clauser–Horne–Shimony–Holt theorem, the Kochen–Specker theorem, and Fine's theorems all generate
 395 strong restrictions on the possible form that a separable system can have, and their violation frequently
 396 entails contextual behaviour. Here we shall only explore some of the more accessible examples. The
 397 interested reader is encouraged to consult the many different references cited here and elsewhere for
 398 further details.

399 3.2.1. Context in Measurement

400 Quantum measurements are frequently shown to behave in a contextual manner using a violation of
 401 the Law of Total Probability as a test [52].

For example, Busemeyer *et al.* [54] resolve the well known Linda Problem, which arises from
 applying the standard conjunction rule of probability to human reasoning. This rule tells us that the
 probability of some event A occurring in conjunction with a specific event X_j is smaller than that of the
 same event occurring in conjunction with a more general event $\sum_j X_j$:

$$P(AX) = \sum_j P(AX_j) \Rightarrow P(AX) \geq P(AX_j) \forall j. \quad (1)$$

402 This basic law of probability is frequently violated by humans across a wide range of demographics
 403 (including educational ones). Such violations are commonly generated via a story that proceeds
 404 something like the following:

405 *Linda is 31 years old, single, outspoken, and very bright. She majored in philosophy.*
 406 *As a student, she was deeply concerned with issues of discrimination and social justice, and*
 407 *also participated in anti-nuclear demonstrations. Which is more probable?*

408 1. *Linda is a bank teller.*

409 2. *Linda is a bank teller and is active in the feminist movement.*

410 A large majority of people (85% in the original case presented by Tversky and Kahneman [80])
 411 choose the second option, thus making statements that are more specific than necessary (e.g. $P(AX) <$

412 $P(AX_j))$ hence *less* likely according to standard probability. We see that the preceding story is affecting
 413 the way in which people reason probabilistically about Linda. This violation of the conjunction rule
 414 is well explained by a quantum model which uses projections in geometric spaces, and interference
 415 between different framings of a problem to explain how the context in which human subjects form a
 416 model of ‘Linda’ is affected by the context of the preceding story. This model is used to explain a wide
 417 range of effects traditionally considered disparate in psychology and cognitive science, including the
 418 disjunction fallacy, and the hot hand fallacy [52,54,55,81,82]. The standard approach followed in these
 419 scenarios involves finding a dataset where a Law of Total Probability is violated, and then fitting the
 420 data with quantum interference terms which adjust the probabilities in the model to fit the experimental
 421 results (see e.g. Busemeyer and Bruza [52] for a general introduction).

422 It might be claimed that this form of contextuality is not particularly interesting; the context of a
 423 stimulus is affecting a behavioural response (i.e. the decision of a subject about Linda’s status), which
 424 would be expected by any researcher in a field such as psychology. However, the quantum formalism
 425 offers a methodology that shows promise for describing a wide range of contextual effects within a
 426 unified formalism, rather than an ad hoc and incremental set of approaches. More examples as we
 427 continue will help to demonstrate this potential.

Another form of contextuality upon measurement is exhibited by systems which display *order effects*
 (meaning that the order in which two measurements are performed affects the outcome). Wang and
 Busemeyer [83] discuss a number of well known scenarios, unifying them in an approach based upon
 quantum probability. For example, Moore [84] showed that asking subjects about the trustworthiness
 of Bill Clinton and then Al Gore reduced Gore’s rating (down to 60% from a value of 68%, obtained
 when Gore was rated first). That is, in the comparative context of Clinton, Gore seems less trustworthy.
 Clinton was similarly rated as more trustworthy when subjects were asked to rate Gore first (57% from a
 non-comparative result of 50%). This effect was modelled by Wang and Busemeyer [83] using projection
 operators to represent the probability of responding yes to question A (e.g. “Is Al Gore trustworthy?”) as
 \mathbf{P}_{Ay} (similarly that of responding no to A as \mathbf{P}_{An}). Asking one question is seen to project the cognitive
 state into a subspace, which then changes the probabilities of a subject answering yes to question B (as
 was discussed above for the general model). Wang and Busemeyer [83] use the formalism of QT to
 define an equality which must be satisfied by any system exhibiting pure quantum behaviour, the *q-test*:

$$q = P_{AB} - P_{BA} = 0 \quad (2)$$

428 where $P_{AB} = P(AyBn) + P(AnBy)$ and $P_{BA} = P(ByAn) + P(BnAy)$ which are two probabilities
 429 referring to the probability of having different answers to two questions (A and B) in the orders AB
 430 and BA respectively. They use this test to explain the results reported in Moore [84], thus unifying the
 431 violation of the LTP discussed above, with that of order effects in psychology.

432 A further experiment, discussed by White *et al.* [85] demonstrates that the *constructive* role of
 433 measurement is likely to be causing the change in probabilities that arise in these scenarios. This paper
 434 introduces a very simple paradigm, where subjects are exposed to two images in a row, with half of the
 435 subjects asked to articulate their impressions about the first image before being shown the second, and
 436 all subjects asked to articulate their impressions about the second image. This experiment shows that
 437 even a slight modification in the instructions given to a subject can have a significant impact upon their

438 response, even keeping all other factors constant (in this case order and images). Such a modification
439 is most naturally treated as a context if we take the geometric model discussed above. Asking a subject
440 to express their impression about the first image effectively performs a measurement on that subject's
441 cognitive state, and this in turn modifies their state. The next measurement is performed upon a different
442 system.

443 This section has discussed a number of different types of context, along with a consistent model that
444 can be used to describe them. Furthermore, this model provides natural tests that can be used to determine
445 whether contextuality is being displayed by the system under consideration or not. However, this is only
446 a first step towards what we might call a Contextualised Generalised Systems Theory. A second set
447 of models and tests come from the quantum formalism when it is applied to systems which consist of
448 multi-component states. These tests can be used to discover whether the system should be considered
449 using a reductive model or not, and while they are related to the tests and models discussed in this section
450 (as they still involve measurement), they add to the formalism by providing further information about
451 the internal behaviour of the system (i.e. between the components).

452 3.2.2. Bell-type theorems

453 What happens when we combine two component systems into one joint system? The quantum
454 formalism has a well developed mechanism for combining systems, using the tensor product and time
455 evolution operations [49]. However, once two originally separate systems interact, can we still model
456 them as separable systems? QT has provided a highly sophisticated toolkit for considering questions
457 such as these.

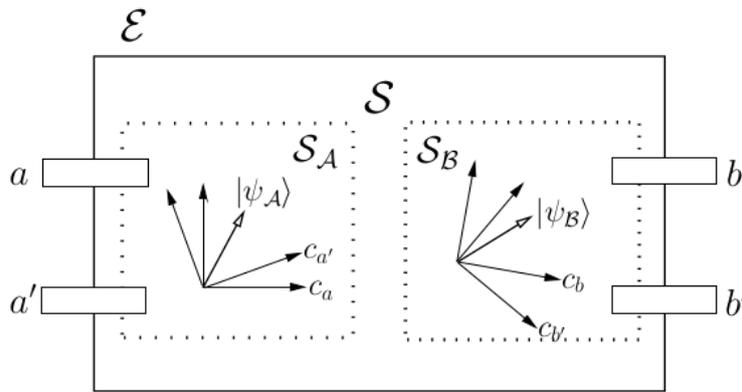
458 Figure 3 depicts a hypothetical system \mathcal{S} , in an environment \mathcal{E} , which consists of two components \mathcal{S}_A
459 and \mathcal{S}_B , that were originally separate (or that we have perhaps imagined could be separated) but have
460 since interacted. There are many questions that can be asked about this system: can \mathcal{S}_A and \mathcal{S}_B still be
461 regarded as separate or do they somehow influence one another? Would a consideration of the combined
462 system $\mathcal{S}_A \oplus \mathcal{S}_B \oplus \mathcal{E}$ give the same specification of behaviour as $\mathcal{S} \oplus \mathcal{E}$? What components of this
463 system exhibit causal interdependencies? QT allows us to move such questions from what are largely
464 philosophical discussions and into the experimental realm.

465 While it is generally assumed that systems are by definition separable in a well defined manner
466 from their environments, a similar separation between \mathcal{S}_A and \mathcal{S}_B is not something that can be
467 straightforwardly achieved in QT, even when there is no apparent causal connection between the two
468 components.

469 For example, suppose that two different experiments can be carried out upon each of the presumed
470 subsystems, which will answer a set of 'questions' with binary outcomes. We shall represent these
471 questions using four possible measurement settings, consisting of two alternative questions asked
472 of either sub-component. Thus, a choice of two experimental settings a or a' can be applied to
473 sub-component \mathcal{S}_A , and similarly b or b' can be applied to sub-component B . Each of these experimental
474 questions lead to a binary outcome (e.g. a detector clicks or it does not) which represents either a 'yes'
475 or a 'no' answer to the question asked of the system. For the sake of generality we shall denote these
476 responses as $+1$ or 0 respectively, they form a set of random variables that we shall label as $A, A', B,$

477 and \mathbf{B}' . It is now possible to consider the notion of the probability distribution over these outcomes;
 478 what characteristics will be possessed by the random variables describing this system?

Figure 3. A potentially compositional system \mathcal{S} , consisting of two assumed sub-components $\mathcal{S}_A = |\psi_A\rangle$ and $\mathcal{S}_B = |\psi_B\rangle$. \mathcal{S} can perhaps be understood in terms of a mutually exclusive choice of experiments upon those sub-components. Two alternative experimental settings probe either proposed sub-component, represented by a or a' for sub-component \mathcal{S}_A , and b, b' for sub-component \mathcal{S}_B . Each of these experimental settings corresponds to a context $c_a, c_{a'}, c_b, c_{b'}$ which is used to represent the sub-system (and sometimes the system as well) in that context, using the formalism introduced in figure 2.



479 As with many systems, the outcomes of our experiments will have a statistical distribution over all
 480 available outcomes, and this can be used to determine whether the sub-components can be considered as
 481 isolated, influencing one another, or in some sense irreducible. Frequently, joint probability distributions
 482 such as $P(\mathbf{A}, \mathbf{A}', \mathbf{B}, \mathbf{B}')$ are used to model the behaviour of systems like that represented in figure 3,
 483 however, it has been shown that this joint probability does not exist for certain quantum [75,86] and
 484 psychological systems [17,52,87]. When such behaviour is evident, we have clear reason to suppose
 485 that the system under examination is contextual; experiments performed upon sub-system \mathcal{S}_B affect the
 486 results of experiments performed upon sub-system \mathcal{S}_A , even though the two sub-systems were presumed
 487 independent. Thus, the context of sub-system \mathcal{S}_A , as represented by sub-system \mathcal{S}_A , can have a well
 488 defined influence upon its behaviour which is not causal in any of the more traditional understandings.

It is possible to derive a number of restrictions on the probability distributions that must be satisfied by a *separable system*. For example we could define such a system as one for which experiments performed at \mathcal{S}_A will not affect those performed at \mathcal{S}_B and vice versa. More specifically, a person committed to reductive modelling would normally assume that the result of running experiments a or a' do not depend upon the experimental settings used on subsystem \mathcal{S}_B (i.e. b or b'), and that the results of experimentally interacting with subsystem \mathcal{S}_B do not depend upon the experimental settings applied to \mathcal{S}_A (i.e. a or a'). It is possible to construct a joint probability describing this state of affairs, and how it might depend upon a set of hidden parameters, or latent variables, denoted λ , which is assumed to have a normalised probability distribution $\rho : \int d\lambda \rho(\lambda) = 1$. The joint probability for experimental arrangement a, b becomes

$$P(a, b) = \int d\lambda \rho(\lambda) \mathbf{A}(a, \lambda) \mathbf{B}(b, \lambda) \quad (3)$$

and a similar set of relationships can be constructed for all experimental arrangements. Simple algebra allows us to form a number of inequalities that result from this assumption. For example, we can derive the Clauser–Horne–Shimony–Holt (CHSH) inequality [88], which has become somewhat notorious in the field of quantum physics:

$$|P(a, b) - P(a, b')| + |P(a', b) + P(a', b')| \leq 2. \quad (4)$$

489 This is a very general statement about the possibility of separating a system into objective components
 490 which interact only via the proposed variable λ . If this inequality is violated, then this separation is
 491 impossible. It is worth emphasising the generality of this result. While it was originally obtained in the
 492 field of quantum theory, the derivation of (4) makes no assumptions as to the nature of the system that is
 493 modelled by the probabilistic framework that it proposes, merely as to the potential separability of \mathcal{S} .

494 This class of tests, and their more advanced forms have been applied to both language [17,89,90] and
 495 biological systems [15]. It has also been shown to have a close connection with the notion of selective
 496 influences in psychology [87]. We see that very clear tests can be constructed to determine whether two
 497 apparently separate systems can indeed be modelled reductively, or not.

498 There are a number of extensions of this test. Many of them either use multi-partite systems, or
 499 describe two-partite systems with a larger number of operators [50,75,91–93]. Many of these extensions
 500 allow for the construction of direct counterfactual scenarios, where if a particular experimental outcome
 501 is realised then a separable model of the system becomes impossible. The Greenberger–Horne–Zeilinger
 502 (GHZ) [92] and Hardy constructions [94], as well as the Kochen–Specker theorem [50,95] would provide
 503 very strong additional tests about non-separability if they could be adapted and generalised beyond
 504 standard QT. While such tests are yet to be realised in a quantum-like model they provide a potentially
 505 fruitful avenue for future work.

506 3.3. *Quantum Models of Emergence*

507 Standard QT (or Quantum Mechanics) does not describe the emergence of novelty. Indeed, physicists
 508 found it necessary to extend the formalism of QT with Quantum Field Theory (QFT) when they started
 509 to model situations such as the creation and annihilation of particles within physics. In contrast to
 510 standard QT, which preserves the number of particles in a system and hence cannot describe the complex
 511 interactions occurring in much of the physical world (such as for example the behaviour of atomic
 512 nuclei), QFT allows for the description of a number of *inequivalent* representations of the same physical
 513 system [13]. This means that a QFT can model systems with many different ground states (lowest
 514 energy states), a far more natural state of affairs for complex systems, as these often have a range of
 515 stable configurations. If a QFT exhibits spontaneous symmetry breaking, meaning that the symmetry
 516 of the dynamics of the system is different from that of the ground state, then collective excitations can
 517 arise (termed Nambu–Goldstone modes [79,96]) corresponding to the number of broken symmetries.
 518 These modes are massless, and hence long range, which means that information can be transmitted very
 519 efficiently in such theories. It is also possible to construct dissipative QFT's, which take into account the
 520 generally open nature of a complex system and has the added benefit of providing an essentially infinite
 521 capacity for the system. Thus in Vitiello's QFT brain model [13] the memory capacity of the brain is

522 practically infinite due to the openness of our interactions with the world; there is an inexhaustible supply
523 of different stable memory states and a way of changing from one to the other in time.

524 While those approaches that use standard QT are modelling the context of the system in terms of
525 different observations, it seems likely that QFT can provide science with a genuine theory of ontological
526 emergence [21,41,41]. While a general theory is yet to be developed, initially promising results have
527 been found describing the brain [13], stock market dynamics [71], conceptual combination [97] and
528 differentiation [15,21].

529 Stepping back, it is necessary to briefly consider where exactly a quantum field theoretic model of
530 ontological emergence could fit into the larger understanding of emergence, and into systems theory as a
531 whole. One overarching understanding is provided by Atmanspacher [6], who identifies four classes of
532 relations between two levels in a system exhibiting emergent behaviour. Each of these classes lead to very
533 different expectations of emergence, as they arise from a different understanding of how the description
534 of features at one level of a system relate to those at a higher level. Thus, (i) if the description at the
535 low level is necessary and sufficient for a complete understanding at the higher level, then the system
536 is reductive (implying no emergence at all); (ii) If the low level is neither necessary nor sufficient for
537 description at the higher level, then there are no relevant conditions for connecting the two levels (this
538 is termed radical emergence). The two more interesting categories come from dropping one of the two
539 sufficiency criteria: Atmanspacher [6] claims that (iii) supervenience results from the dropping of the
540 necessary condition, and (iv) contextual emergence as resultant from dropping the sufficiency condition.
541 Thus, in the description of a contextually emergent system, ontological emergence can occur, but a model
542 that refers only to the lower level will not prove sufficient for describing the dynamics of the system at the
543 higher level. Contextual systems which require an epistemic cut will fall into this class of *contextually*
544 *emergent systems*, as they require extra information beyond that of the original system to be incorporated
545 into a model which captures their full behaviour.

546 This brings us to our final discussion; how do all of the concepts that we have discussed so far fit
547 together into an overarching framework that could drive a new Contextualised General Systems Theory?

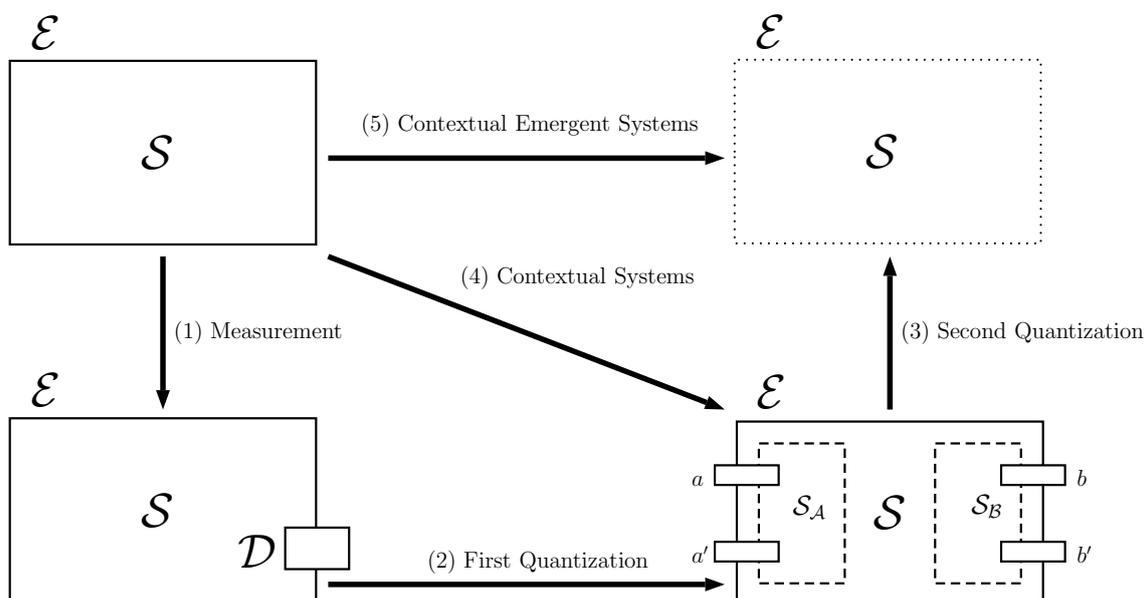
548 **4. Towards a General Theory**

549 At the beginning of this discussion we started by examining the notion of a system. We saw that while
550 a system in an environment is easy to imagine, the reality is not so simple. We quickly found examples
551 of systems which exhibit a variety of contextual responses to measurement and their environment, which
552 makes it markedly difficult to draw a clean line between the system and the environment. Many of these
553 systems are termed complex, however, the designation of a system as complex often depends upon what
554 aspect of it we are interested in modelling; it is necessary to specify the level of description before we can
555 make statements as to a system's complexity. We then sought to examine the manner in which system
556 contextuality affects measurement results and the advantage of the quantum formalism became apparent.
557 It is a formalism that recognises the manner in which our interactions with a contextually dependent
558 system will affect the results of measurements that we perform upon it. The geometric probabilities
559 used in QT link experimental manipulations made by an observer with the behaviour exhibited by the
560 system, which provides an invaluable modelling tool. A number of different proposals have been made

561 as to why QT should be used to model systems that are not traditionally deemed physical (see e.g.
 562 [13,15,52,53,98,99]). Here, I have attempted to show that QT provides us with a methodology that
 563 can consistently approach the notion of contextuality, between any combination of system components,
 564 experiments, and environments. QT thus provides a possibility for unifying our understanding of a
 565 number of hitherto disparate contextuality effects, across a wide range of fields. Of course such an
 566 understanding requires much more work before it can be considered as complete; an ongoing program
 567 of research is required.

568 One particularly important clarification will require a much more sophisticated understanding of
 569 quantum operators for non-physical systems. QT arose in physics only after a notion of classical
 570 measurement was defined. This meant that a dynamics had been defined classically, which mapped
 571 naturally into QT via Hamiltonians, Energy, Pauli matrices etc. Each one of these concepts have a
 572 well-defined meaning in physics, but this is much more difficult to discern in the quantum-like world
 573 (i.e. beyond physics). This makes many powerful analytical techniques inaccessible to the field, at
 574 least for now. For example, it is very difficult to understand how a quantum-like system will evolve in
 575 time without a Hamiltonian. While dynamics can perhaps be reverse engineered (say by performing the
 576 same measurement over a series of time steps), the very contextuality of these systems makes it hard to
 577 know what is causing changes in experimental results. It seems likely that many quantum-like systems
 578 will not be modelled via the standard physical technique of quantization (where a classical system is
 579 identified and the operators are then subject to a well defined procedure which results in a quantum
 580 system). Quantum-like systems are being modelled by the quantum formalism precisely because they
 581 *never* exhibited non-contextual behaviour, but this makes it very difficult to develop even a quantum
 582 formalism for these systems.

Figure 4. A Contextual General Systems Theory would explain all of the relationships between the below four types of systems. Importantly, it would provide natural explanations of how paths (4) and (5) could be followed without assuming a classical (i.e. non-contextual) model at the outset.



583 Referring to Figure 4, this would imply that we need a procedure for following mapping (4) directly
584 (i.e. skipping the measurement to first quantization paths). This is a difficult proposition, and it is made
585 more difficult when we consider the manner in which systems of type (c) are likely to be modelled most
586 productively by following path (5), which would require moving directly from acknowledging a system
587 exits to the recognition that it has open boundaries and is exhibiting emergent behaviour. We need new
588 techniques. These would provide a direct map from the identification of a system to follow either:

589 **Path (4):** A contextual model of its behaviour which did not require the construction of a classical model
590 which was then subject to quantization (currently only understood via the alternate path (1)→(2)
591 route).

592 **Path (5):** A contextual model of emergent behaviour which also left out the second quantization option.

593 If direct paths could be found then they would allow for models of contextual systems to be constructed
594 without following the standard reductive modelling methodology, where we assume a set of objects, and
595 then gradually relax our assumptions about their behaviour (through first and second quantization).

596 One extant theory almost follows path (5). Modern path integral forms of Quantum Field Theory
597 [96,100] proceed by identifying a system, and then modelling correlations between two points (which
598 can correspond to experimental settings). Thus, modern QFT proceeds directly to the description of
599 contextual emergent systems, from the identification of a classical dynamics. Essential to this move
600 is the identification of a set of groups and symmetries. Similarly, even following path (4) requires
601 the identification of a group structure for the description of both time evolution and certain associated
602 measurements (e.g. spin in standard QT). However, this is no easy challenge. There is no guarantee that
603 the systems of biology, cognition or society will follow the same symmetries as those of physics. Indeed,
604 it is quite likely that they will prove to be far more complex.

605 It is worth noting that the schema proposed here is not a hierarchy of theories (such as the one
606 proposed by Marr, see section 1.3) or the varying approaches to understanding emergence. Rather,
607 figure 4 is a set of relationships between different conceptualisations of a system. Different systems will
608 be most naturally modelled at different positions in this diagram, but the relationships show us what kind
609 of an effort would be involved in ‘scaling up’ the complexity away from the simple $\mathcal{S} \oplus \mathcal{E}$ assumption.
610 It also goes some way towards demonstrating what types of behaviours would need to be exhibited by a
611 system at the level of analysis that we had chosen for it before such a move became necessary.

612 5. Conclusions

613 Formalising the notion of context is not impossible, but it will require sophisticated new mathematical
614 techniques. It also requires a thorough re-examination of the assumptions that we make when attempting
615 a scientific explanation. The fact that a system does not display objective responses to measurement need
616 not imply that it is beyond the realms of science; QT provides a direct counterexample, and much can be
617 learned from a careful consideration of the system of techniques that make up this approach.

618 Here, I have attempted to show that a unified approach to contextuality is possible. Taking inspiration
619 from the quantum formalism we can start to understand many different types of contextual system. We
620 can also start to utilise a range of tests that can be used to determine whether a system is contextual, and

621 a formalism that can help us to model its behaviour if it is. While I hope that the ideas discussed in this
622 paper have sketched out a range of possibilities, much work remains to be done. However, it seems like
623 a Contextualised General Systems Theory is possible, and not too far away on the horizon.

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632 **Conflicts of Interest**

633 I declare no conflict of interest.

634 **References**

- 635 1. von Bertalanffy, L. *General System Theory: Foundations, Development, Applications*; George
636 Braziller: New York, 1968.
- 637 2. Pouvreau, D.; Drack, M. On the history of Ludwig von Bertalanffy's "General Systemology", and
638 on its relationship to cybernetics. *International Journal of General Systems* **2007**, *36*, 281–337.
- 639 3. Fried, H.M. *Functional Methods and Models in Quantum Field Theory*; MIT, 1972.
- 640 4. Backlund, A. The definition of system. *Kybernetes* **2000**, *29*, 444 – 451.
- 641 5. Schaffner, K.F. Approaches to Reduction. *Philosophy of Science* **1967**, *34*, pp. 137–147.
- 642 6. Atmanspacher, H. Contextual Emergence from Physics to Cognitive Neuroscience. *Journal of*
643 *Consciousness Studies* **2007**, *14*, 18–36.
- 644 7. West-Eberhard, M.J. *Developmental Plasticity and Evolution*; Oxford University Press, 2003.
- 645 8. Piersma, T.; Gils, J.A.V. *The Flexible Phenotype: A Body-Centred Integration of Ecology,*
646 *Physiology, and Behaviour*; Oxford University Press, 2011.
- 647 9. Bond, R.; Smith, P.B. Culture and Conformity: A Meta-Analysis of Studies Using Asch's (*1952b, 1956*)
648 Line Judgment Task. *Psychological Bulletin* **1996**, *119*, 111–137.
- 649 10. Bell, J.S. *Speakable and unspeakable in quantum mechanics*; Cambridge University Press:
650 Cambridge, 1987.
- 651 11. Wilson, K.G. Confinement of Quarks. *Physical Review D* **1974**, *10*, 2445–2459.
- 652 12. Marshak, R.E. *Conceptual Foundations of Modern Particle Physics*; World Scientific: Singapore,
653 1993.
- 654 13. Vitiello, G. *My Double Unveiled*; John Benjamins Publishing Company: Amsterdam, 2001.
- 655 14. Nicholis, G.; Prigogine, I. *Self-Organization in Non-Equilibrium Systems: From Dissipative*
656 *Structures to Order through Fluctuations*; J. Wiley and Sons., 1997.

- 657 15. Kitto, K.; Kortschak, R.D. Contextual Models and the Non-Newtonian Paradigm. *Progress in*
658 *Biophysics & Molecular Biology* **2013**, *113*, 97–107.
- 659 16. Mitchell, J.; Lapata, M. Composition in distributional models of semantics. *Cognitive Science*
660 **2010**, *34*, 1388–1429.
- 661 17. Bruza, P.; Kitto, K.; Ramm, B.; Sitbon, L. A probabilistic framework for analyzing the
662 compositionality of conceptual combinations **2012**. Under Review.
- 663 18. Augoustinos, M.; Walker, I.; Donaghue, N. *Social Cognition*, 2nd ed.; Sage: London, 2006.
- 664 19. Tversky, A.; Kahneman, D. The framing of decisions and the psychology of choice. *Science*
665 **1981**, *211*, 453–458.
- 666 20. Albert, R.; Barabási, A.L. Statistical mechanics of complex networks. *Reviews of Modern*
667 *Physics* **2002**, *74*, 47–97.
- 668 21. Kitto, K. High End Complexity. *International Journal of General Systems* **2008**, *37*, 689–714.
- 669 22. Bitbol, M. Ontology, matter and emergence. *Phenomenology and the Cognitive Science* **2007**,
670 *6*, 293–307.
- 671 23. Minati, G.; Pessa, E. *Collective Beings; Contemporary Systems Thinking*, Springer: New York,
672 2006.
- 673 24. Rosen, R. *Life Itself: A comprehensive inquiry into the nature, origin, and fabrication of life;*
674 *Complexity in Ecological Systems Series*, Columbia University Press: New York, 1991.
- 675 25. Mitchell, M. *Complexity: A Guided Tour*; Oxford University Press: Oxford, U.K., 2009.
- 676 26. Miller, J.H.; Page, S.E. *Complex Adaptive Systems: An Introduction to Computational Models of*
677 *Social Life*; Princeton University Press, 2007.
- 678 27. O'Neill, R.V.; DeAngelis, D.L.; Waide, J.B.; Allen, T.F.H. *A Hierarchical Concept of*
679 *Ecosystems*; Vol. 23, *Monographs in Population Biology*, Princeton University Press: Princeton,
680 New Jersey, 1986.
- 681 28. Marr, D.; Poggio, T. From Understanding Computation to Understanding Neural Circuitry.
682 Artificial Intelligence Laboratory. A.I. Memo. AIM-357, Massachusetts Institute of Technology,
683 1976. Available for download at: <http://dspace.mit.edu/handle/1721.1/5782>.
- 684 29. McClamrock, R. Marr's three levels: A re-evaluation. *Minds and Machines* **1991**, *1*, 185–196.
- 685 30. Anderson, P.W. More Is Different. *Science* **1972**, *177*, 393–396.
- 686 31. Kampis, G. The Inside and Outside Views of Life. *Advances in Artificial Life*; Moran,
687 F.; Moreno, A.; Merelo, J.; Chacon, P., Eds. Springer, 1995, Third European Conference on
688 Artificial Life Granada, Spain, June 4–6, 1995, pp. 95–102.
- 689 32. Pattee, H.H. The physics of symbols: bridging the epistemic cut. *BioSystems* **2001**, *60*, 5–21.
- 690 33. Bell, J.S. Six possible worlds of quantum mechanics. In *Speakable and unspeakable in quantum*
691 *mechanics*; Cambridge University Press: Cambridge, 1987; pp. 181–195.
- 692 34. Barabási, A.L.; Oltvar, Z. Network biology: understanding the cell's functional organization.
693 *Nature Reviews: Genetics* **2004**, *5*, 101–113.
- 694 35. Bouchaud, J.P. Economics needs a scientific revolution. *Nature* **2008**, *455*, 1181.
- 695 36. Alon, U. *An introduction to systems biology: design principles of biological circuits*; Chapman
696 & Hall, 2006.

- 697 37. Alon, U. Network motifs: theory and experimental approaches. *Nature Reviews Genetics* **2007**,
698 8, 450–461.
- 699 38. Billari, F.C.; Fent, T.; Prskawetz, A., Eds. *Agent-Based Computational Modelling: Applications*
700 *in Demography, Social, Economic and Environmental Sciences (Contributions to Economics)*;
701 Physica-Verlag: Heidelberg, 2006.
- 702 39. Epstein, J.M. *Generative Social Science: Studies in Agent-Based Computational Modeling*;
703 Princeton Studies in Complexity, Princeton University Press, 2007.
- 704 40. Pessa, E. Self-Organization and Emergence in Neural Networks. *Electronic Journal of*
705 *Theoretical Physics* **2009**, 6, 269–306.
- 706 41. Kitto, K. Modelling and Generating Complex Emergent Behaviour. PhD thesis, School of
707 Chemistry Physics and Earth Sciences, The Flinders University of South Australia, 2006.
- 708 42. Mruck, K.; Wolff-Michael, R.; Breuer, F., Eds. *Forum: Qualitative Social Research*; Vol. 3,
709 *Subjectivity and Reflexivity in Qualitative Research I*, 2002.
- 710 43. Tomasello, M. *The Cultural Origins of Human Cognition*; Harvard University Press, 1999.
- 711 44. Jenkins, J.H.; Barrett, R.J. *Schizophrenia, Culture, and Subjectivity: The Edge of Experience*;
712 Cambridge University Press: New York, 2004.
- 713 45. Gärdenfors, P. *Conceptual Spaces: The Geometry of Thought*; MIT Press, 2000.
- 714 46. West-Eberhard, M.J. Phenotypic Plasticity and the Origins of Diversity. *Annual Review of*
715 *Ecology and Systematics* **1989**, 20, 249–278.
- 716 47. Thom, R. *Structural Stability and Morphogenesis*; W. A. Benjamin: Reading, Massachusetts,
717 1975.
- 718 48. Kampis, G. *Self-Modifying systems in biology and cognitive science*; Pergamon Press Inc:
719 Oxford, 1991.
- 720 49. Isham, C.J. *Lectures on Quantum Theory*; Imperial College Press: London, 1995.
- 721 50. Mermin, N.D. Hidden variables and the two theorems of John Bell. *Reviews of Modern Physics*
722 **1993**, 65, 803–815.
- 723 51. Ballentine, L. *Quantum Mechanics: A modern development*; World Scientific, 1998.
- 724 52. Busemeyer, J.; Bruza, P. *Quantum Models of Cognition and Decision*; Cambridge University
725 Press, 2012.
- 726 53. Khrennikov, A.Y. *Ubiquitous Quantum Structure: From Psychology to Finance*; Springer, 2010.
- 727 54. Busemeyer, J.; Pothos, E.; Franco, R.; Trueblood, J. A Quantum Theoretical Explanation for
728 Probability Judgment Errors. *Psychological Review* **2011**, 118, 193–218.
- 729 55. Pothos, E.M.; Busemeyer, J.R. A quantum probability explanation for violations of ‘rational’
730 decision theory. *Proceedings of the Royal Society B* **2009**, 276, 2171–2178.
- 731 56. Mogiliansky, A.L.; Zamir, S.; Zwirn, H. Type indeterminacy: A model of the
732 KT(Kahneman-Tversky)-man. *Journal of Mathematical Psychology* **2009**, 53, 349 – 361.
- 733 57. Yukalov, V.I.; Sornette, D. Decision theory with prospect interference and entanglement. *Theory*
734 *and Decision* **2011**, 70, 283–328.
- 735 58. Khrennikova, P.; Haven, E.; Khrennikov, A. An Application of the Theory of Open Quantum
736 Systems to Model the Dynamics of Party Governance in the US Political System. *International*
737 *journal of theoretical physics* **2014**, 53, 1346–1360.

- 738 59. Kitto, K.; Boschetti, F. Attitudes, Ideologies and Self-Organisation: Information Load
739 Minimisation in Multi-agent Decision Making. *Advances in Complex Systems* **2013**,
740 *16*, 1350029.
- 741 60. Gabora, L.; Aerts, D. Contextualizing Concepts using a Mathematical Generalization of the
742 Quantum Formalism. *Journal of Experimental and Theoretical Artificial Intelligence* **2002**,
743 *14*, 327–358.
- 744 61. Aerts, D.; Gabora, L. A theory of concepts and their combinations I: the structure of the sets of
745 contexts and properties. *Kybernetes* **2005**, *34*, 151–175.
- 746 62. Bruza, P.; Kitto, K.; Nelson, D.; McEvoy, C. Is there something quantum-like about the human
747 mental lexicon? *Journal of Mathematical Psychology* **2009**, *53*, 362–377.
- 748 63. Nelson, D.L.; Kitto, K.; Galea, D.; McEvoy, C.L.; Bruza, P.D. How Activation, Entanglement,
749 and Search In Semantic Memory Contribute to Event Memory. *Memory and Cognition* **2013**,
750 *41*, 717–819.
- 751 64. Asano, M.; Basieva, I.; Khrennikov, A.; Ohya, M.; Tanaka, Y.; Yamato, I. Quantum-like model
752 of diauxie in *Escherichia coli*: Operational description of precultivation effect. *Journal of*
753 *Theoretical Biology* **2012**, *314*, 130 – 137.
- 754 65. Aerts, D.; Czachor, M.; Gabora, L.; Kuna, M.; Posiewnik, A.; Pykacz, J.; Syty, M. Quantum
755 morphogenesis: A variation on Thom’s catastrophe theory. *Physical Review E* **2003**, *67*, 051926.
- 756 66. Asano, M.; Basieva, I.; Khrennikov, A.; Ohya, M.; Tanaka, Y.; Yamato, I. A model of epigenetic
757 evolution based on theory of open quantum systems. *Systems and Synthetic Biology* **2013**,
758 *7*, 161–173.
- 759 67. Gabora, L.; Kitto, K., *Origins of Mind*; Springer, 2013; Vol. 8, *Biosemiotics*, chapter Concept
760 Combination and the Origins of Complex Cognition.
- 761 68. Gabora, L.; Aerts, D. Evolution as context-driven actualization of potential. *Interdisciplinary*
762 *Science Reviews* **2005**, *30*, 69–88.
- 763 69. Atmanspacher, H.; Filk, T.; Römer, H. Complementarity in bistable perception. In *Recasting*
764 *Reality. Wolfgang Pauli’s Philosophical Ideas and Contemporary Science*; Atmanspacher, H.;
765 Primas, H., Eds.; Springer: Berlin, 2008; pp. 135–150.
- 766 70. Baaquie, B.E. *Quantum Finance: Path Integrals and Hamiltonians for Options and Interest*
767 *Rates*; Cambridge University Press, 2004.
- 768 71. Sornette, D. *Why stock markets crash: critical events in complex financial systems*; Princeton
769 University Press: Princeton, 2003.
- 770 72. Melucci, M. A basis for information retrieval in context. *ACM Trans. Inf. Syst.* **2008**,
771 *26*, 14:1–14:41.
- 772 73. Van Rijsbergen, C. *The Geometry of Information Retrieval*; Cambridge University Press, 2004.
- 773 74. Widdows, D. *Geometry and Meaning*; CSLI Publications, 2004.
- 774 75. Laloë, F. Do we really understand quantum mechanics? Strange correlations, paradoxes, and
775 theorems. *American Journal of Physics* **2001**, *69*, 655–701.
- 776 76. Pitowsky, I. George Boole’s ‘Conditions of Possible Experience’ and the Quantum Puzzle. *The*
777 *British Journal for the Philosophy of Science* **1994**, *45*, 95–125.

- 778 77. Khrennikov, A. Non-Kolmogorov probability models and modified Bell's inequality. *Journal of*
779 *Mathematical Physics* **2000**, *41*, 1768–1777.
- 780 78. Breuer, H.; Petruccione, F. *The Theory of Open Quantum Systems*; Oxford University Press,
781 2007.
- 782 79. Umezawa, H. *Advanced Field Theory: Micro, macro, and thermal physics*; American Institute
783 of Physics: New York, 1993.
- 784 80. Tversky, A.; Kahneman, D. Extensional versus intuitive reasoning: The conjunction fallacy in
785 probability judgment. *Psychological Review* **1983**, *90*, 293–315.
- 786 81. Aerts, D. Quantum structure in cognition. *Journal of Mathematical Psychology* **2009**,
787 *53*, 314–348.
- 788 82. Yukalov, V.I.; Sornette, D. Processing Information in Quantum Decision Theory. *Entropy* **2009**,
789 *11*, 1073–1120.
- 790 83. Wang, Z.; Busemeyer, J.R. A Quantum Question Order Model Supported by Empirical Tests of
791 an A Priori and Precise Prediction. *Topics in Cognitive Sciences* **2013**, pp. 689–710.
- 792 84. Moore, D.W. Measuring New Types of Question-Order Effects: Additive and Subtractive. *The*
793 *Public Opinion Quarterly* **2002**, *66*, pp. 80–91.
- 794 85. White, L.C.; Pothos, E.M.; Busemeyer, J.R. Sometimes it does hurt to ask: The constructive role
795 of articulating impressions. *Cognition* **2014**, *133*, 48 – 64.
- 796 86. Fine, A. Hidden Variables, Joint Probability, and the Bell Inequalities. *Physical Review Letters*
797 **1982**, *48*, 291–295.
- 798 87. Dzhafarov, E.; Kujala, J. Selectivity in probabilistic causality: Where psychology runs into
799 quantum physics. *Journal of Mathematical Psychology* **2012**, *56*, 54–63.
- 800 88. Clauser, J.; Horne, M.; Shimony, A.; Holt, R. Proposed experiment to test local hidden-variable
801 theories. *Physical Review Letters* **1969**, *23*, 880–884.
- 802 89. Kitto, K.; Ramm, B.; Bruza, P.D.; Sitbon, L. Testing for the non-separability of bi-ambiguous
803 words. Proceedings of the AAAI Fall Symposium on Quantum Informatics for Cognitive, Social,
804 and Semantic Processes (QI 2010). AAAI Press, 2010.
- 805 90. Kitto, K.; Bruza, P.D. Tests and Models of Non-compositional Concepts. Proceedings of the
806 34th Annual Conference of the Cognitive Science Society; Miyake, N.; Peebles, D.; Cooper, R.P.,
807 Eds.; Cognitive Science Society: Sapporo, Japan, 2012; pp. 1792–1797.
- 808 91. Greenberger, D.; Horne, M.; Zeilinger, A. Going beyond Bell's theorem. In *Bell's theorem,*
809 *quantum theory, and conceptions of the Universe*; Kafatos, M., Ed.; Kluwer Academic, 1989; pp.
810 73–76.
- 811 92. Greenberger, D.M.; Horne, M.A.; Shimony, A.; Zeilinger, A. Bell's theorem without inequalities.
812 *American Journal of Physics* **1990**, *58*, 1131–1143.
- 813 93. Irvine, W.T.M.; Hodelin, J.F.; Simon, C.; Bouwmeester, D. Realization of Hardy's Thought
814 Experiment with Photons. *Physical Review Letters* **2005**, *95*.
- 815 94. Hardy, L. The EPR argument and nonlocality without inequalities for a single photon. *Annals of*
816 *the New York Academy of sciences* **1995**, *755*, 600–615.
- 817 95. Kochen, S.; Specker, E.P. The problem of hidden variables in quantum mechanics. *Journal of*
818 *Mathematics and Mechanics* **1967**, *17*, 59–87.

- 819 96. Kaku, M. *Quantum Field Theory: a modern introduction*; Oxford University Press: Oxford,
820 1993.
- 821 97. Aerts, D. Quantum structures due to fluctuations of the measurement situations. *International*
822 *Journal of Theoretical Physics* **1993**, 32, 2207.
- 823 98. Atmanspacher, H.; Filk, T.; Römer, H. Weak quantum theory: Formal framework and selected
824 applications **2006**. pp. 34–46.
- 825 99. Kitto, K. Why quantum theory? Proceedings of the Second Quantum Interaction Symposium;
826 Bruza, P.D.; Lawless, W.; van Rijsbergen, K.; Sofge, D.A.; Coecke, B.; Clark, S., Eds. College
827 Publications, 2008, pp. 11–18.
- 828 100. Weinberg, S. *The Quantum Theory of Fields*; Vol. 1, Cambridge University Press: Cambridge,
829 1995.

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